

How statistical tools can help your Proof of Concept studies

Nicolas Bonnet¹

¹SANOFI R&D, CSO, Biostatistics, Early Clinical Development

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Outline

- 1 Introduction & Motivation
- 2 Risks considerations
- 3 Leveraging the information
- 4 Efficiency and cost-effectiveness: adaptive design
- 5 About dose-response characterisation
- 6 Summary and discussions

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- Costs dominated by late-phase development
- Change in development paradigm
 - Exploratory / confirmatory phase

(Modified from Orloff et al. 2009)

- Strategy

- Early Phase research investment until PoC is established

- Confidence to PoC is key

- Cost-effective: early phase research investment

- Early phase research investment

- About the PoC decision

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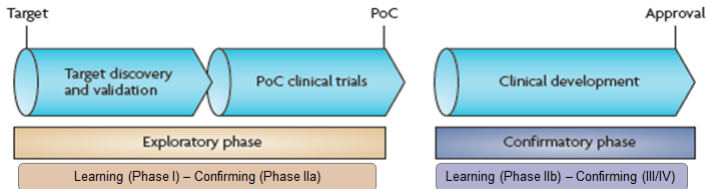
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- Phase I: Dose-toxicity relationship and PoC established

- Phase II: Dose-toxicity relationship and PoC established

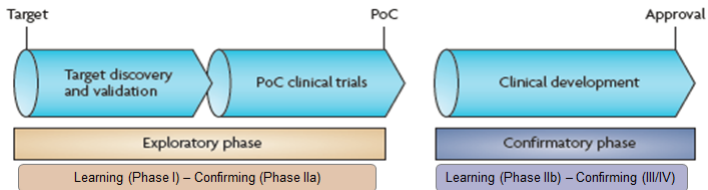
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 - Confidence to further invest in full-development of candidate
 - Confidence to stop a non-promising compound ("fast-to-fail")

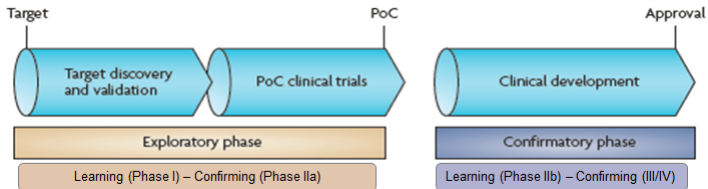
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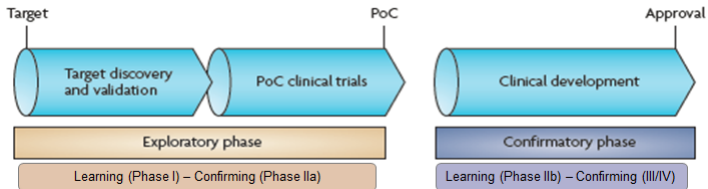
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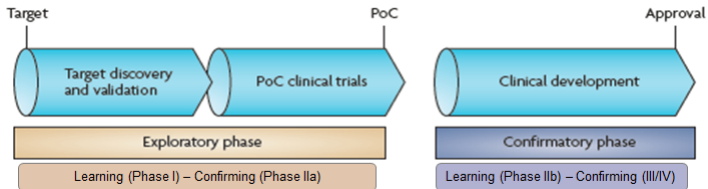
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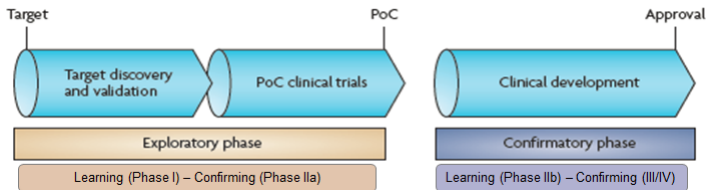


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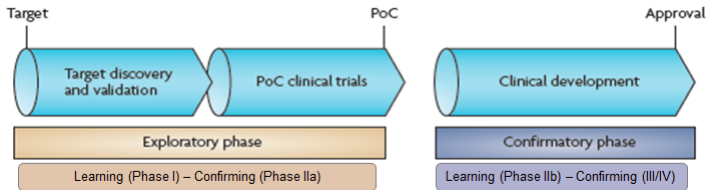


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Proof-of-Concept (Cartwright et al. 2010)

The earliest point in the drug development process at which the weight of evidence suggests that it is "reasonably likely" that the key attributes for success are present and the key causes of failure are absent

- Can take various form depending on the company and the projects
 - Ph IIb dose ranging
 - Ph IIa 2 parallel arms (active MTD vs placebo)
 - Early Proof of Biological Activity ...
- Expectations :
 - Early, time and cost effective demonstration of activity in humans, including an early benefit-risk assessment
 - Increased POS and de-risks further investments
 - PoC study outcome should yield clear "Go/NoGo" decision

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 - ① Clear predefined "Go/No Go" criteria derived from high but reasonable assumptions
 - ② Design adequate to yield
 - High probability of "Go" decision for candidates which truly meet PoC criteria (make this decision reliably)
 - Strong false positive control (stop non promising compound)
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 - Type I error is "lost investment" risk
 - Typically set at 5%
 - Need to be controlled in "fast to fail" paradigm
- Type II error (β): probability of falsely declaring PoC failed
 - Type II error is "lost opportunity" risk
 - Typically set at 10%-20% → corresponds to power of 80%-90% (i.e. $1-\beta$)
 - A power set at 80% means that we have 20% of chance to have a failed study for a compound that reach the predefined target

→ No more chance later on for the compound

→ Are we really to take that risk?

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No more chance to see a new compound

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From a global perspective...

- Type I error
 - Next stage cost versus the risk of missing a true opportunity (of revenue on the market)
 - ⇒ We can relax on α (5% one-sided) or even 10% ?
- Type II error
 - How many compounds do we have as backups in the pipeline ?
 - How many time will we have a Go/NoGo milestone in the development of a given compound?
 - ⇒ use a portfolio-based approach to optimize PoC¹
 - ⇒ we can relax at 80% if we have several backups
- Less regulatory concerns in learning phase
- Under the constraint of a maximal investment (N=100 cap ?)

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A trial case

- After a single and repeated ascending FIM dose
 - We know the maximal tolerated dose (MTD)
- The PoC
 - 2 arms
 - Active vs comparator
 - Relevant effect: $\geq 2mmHg$
 - SD = 3.5
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Classical power

- Once type I error, variability and sample size are chosen, we get the power **conditionally on a specified treatment effect**

The classical power does not quantify the PoS

It is a conditional PoS on the unknown true trt value, $P(\text{Success}|\theta)$

- But the probability of observing such effect ...
- One can sweep across various assumptions on the effect and variability values to assess how robust the power is (for $N=39$ per group)

θ	SD=3	SD=3.25	SD=3.5	SD=3.75
1.5	70%	64%	59%	54%
2	89%	85%	80%	75%
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- Or integrate over possible θ values

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Assurance

- By using the **unconditional PoS**, we take into account the uncertainty around the true underlying treatment effect
 - Define a prior distribution for θ
 - Build a weighted average of the power function with weights from prior distribution

Assurance (Ohagan et al. 2005)

The assurance is the expected power (with respect to the prior)

$$P(\text{Success}) = E(\pi(\theta)) = \int_{\theta} P(\text{Success}, \theta) d\theta = \int_{\theta} P(\text{Success}|\theta) \cdot P(\theta) \cdot d\theta$$

where $\pi(\theta)$ is the power function

- Quantifies the ability of the trial to achieve a success based on available evidence

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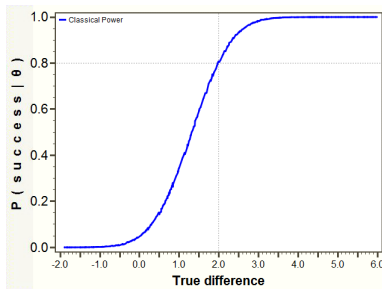
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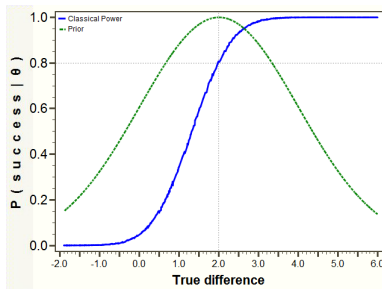
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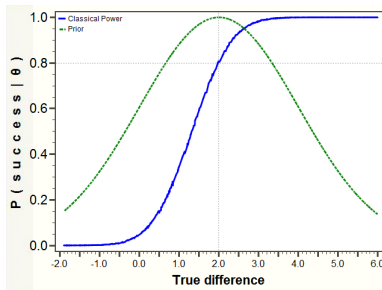
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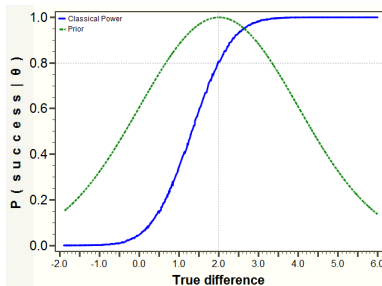
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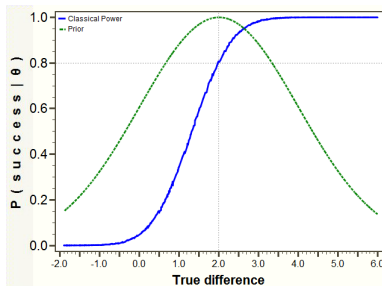
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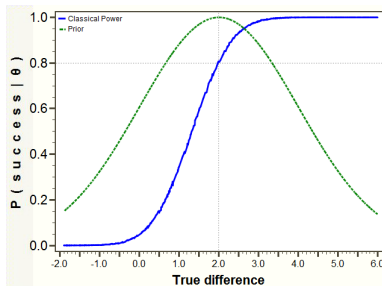
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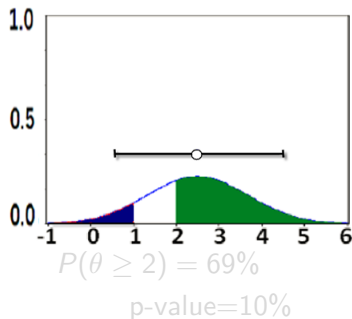
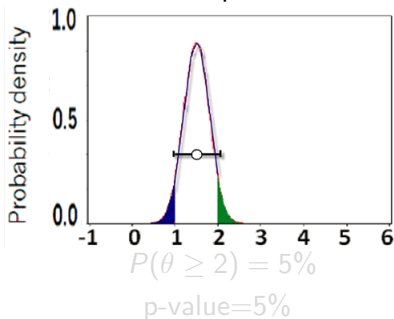
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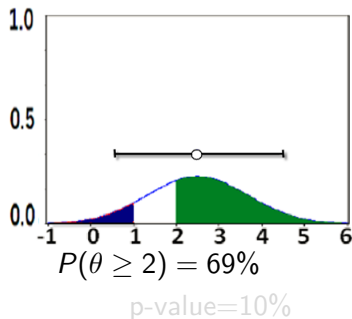
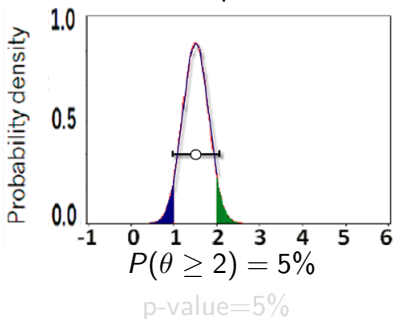
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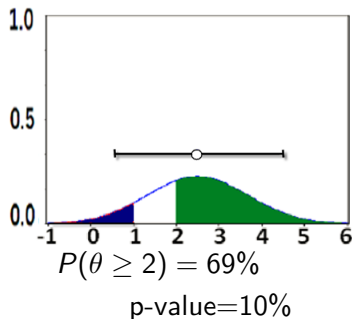
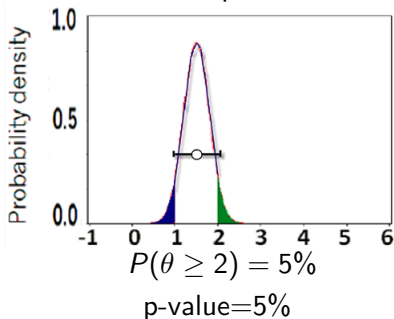
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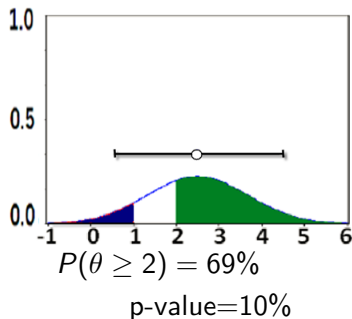
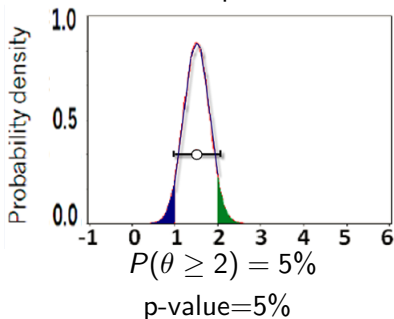
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x

Observed Data \propto **All Data**

Prior distribution $p(\theta)$
(previous study,
literature,...)

Likelihood $p(y|\theta)$
(from experiment)

Posterior
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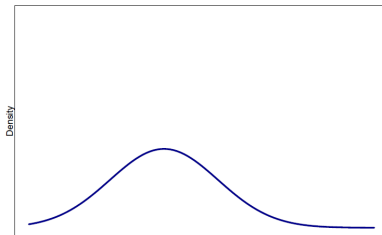
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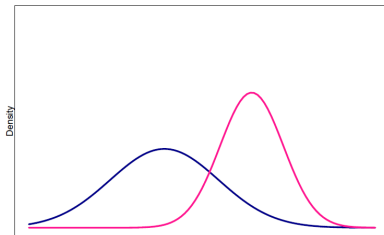
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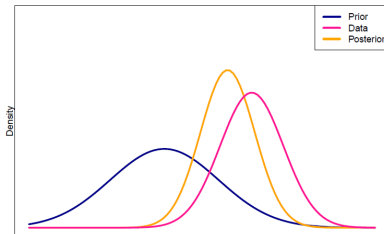
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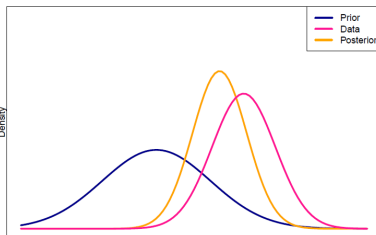
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Non-informative (flat) prior [Active]

Exact inference

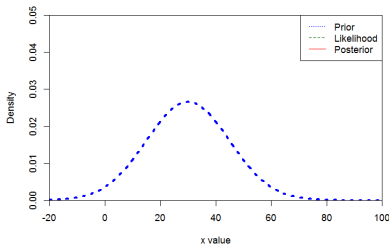
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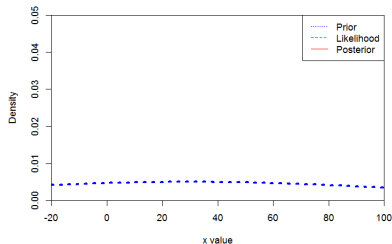
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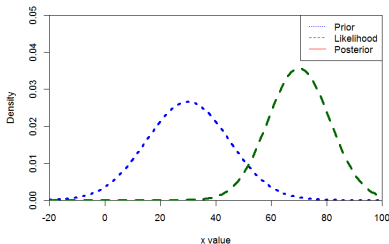


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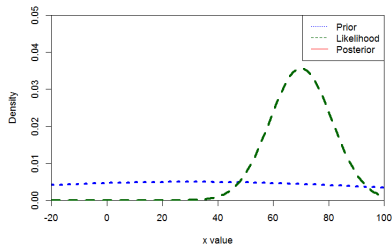
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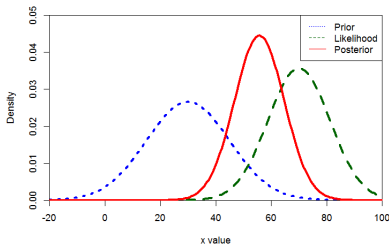


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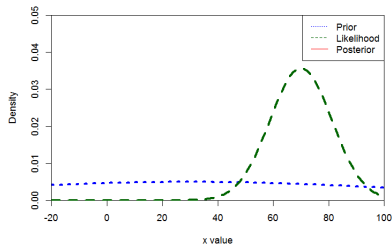
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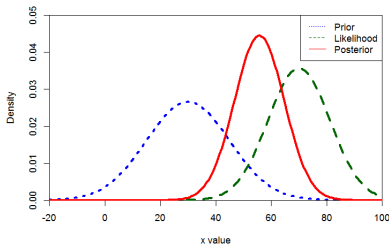


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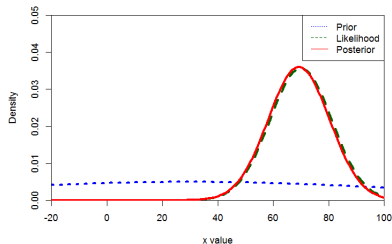
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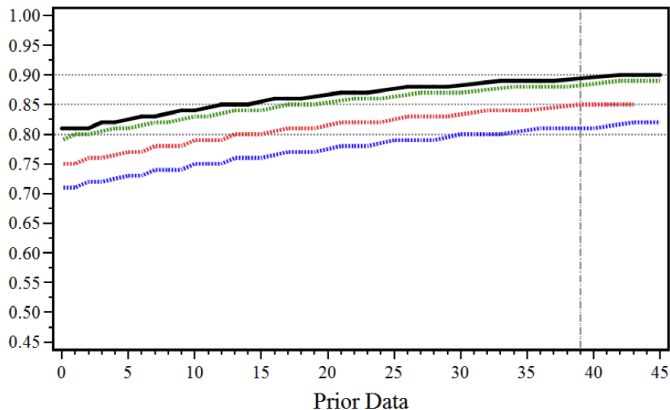
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Gamma parameter [Prior SD 95% CI] ■ G(200;2450)[3.27-3.7] ■ G(20;245)[2.87-4.48]
■ G(40;490)[3.03-4.14] ■ SD= 3.5

Figure : Probability $P(\tau > \tau^* | \text{data})$ VS prior amount of information (q_{0C}) (with $N=39+39$; $P(\tau < 0 | \text{data}) = 0.95$; $\theta=2$)

Table : Probability of success ($P(\tau < 0 | data) = 0.95; \theta = 2$)

SD	Ratio	N _{ACT}	N _C	N _{TOT}	Q _{0c}	PoS
Fixed	1:1	39	39	78	-	80%
$\sim \Gamma(40; 490)$	1:1	39	39	78	39	85%
95%CI=[3.01-4.14]	1:2	52	26	78	26	85%
	1:3	57	19	76	19	80%
					38	87%

- Using bayesian methods leverage the information we have
- Balanced design : PoS increase (even with SD uncertainty)
- Unbalanced design has been proposed
 - to maximize the information on active arm
 - while maintaining good PoS
- Prior elicitation is key : well selected paper
- Many simulations done to assess robustness

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Early phase is an exploratory period for learning

- Continuous update of our knowledge
- Altering study components during the course of the trial, based on accumulated data, could save time and streamline the exploration of the parameters space
- The main regulatory focus in exploratory development phases is on safety
 - much flexibility is allowed into trial features related to the assessment of efficacy, for the purpose of sponsor-internal **decision-making**

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● Context

- 2 arms trial
- Long recruitment due to :
 - Low recruitment rate (difficult patient population)
 - Large number of patients
- Relatively short biomarker readout

● Motivation

- Why should we wait until the end of the trial if partial data demonstrate that the trial is being unlikely to achieve its objective ?
 - Unethical

⇒ Stop for futility !! (or adaptive randomization design)

● Which decisions ?

- Evidence in favor of null or alternative hypotheses at the interim ?
- Evidence in favor of null or alternative hypotheses if additional data are collected ?

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- **P-value**
 - Not the best approach as seen
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20	0.50	0.50
30	0.51	0.50
60	0.49	0.50
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- Relative high posterior probability will not stop the trial whereas we have less chance to conclude as the data accumulate
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Conditional Power : $P(\text{FinalSuccess}|\mu; \sigma)$

- Take into account for how much data remain to be observed
- But one must assume some values of parameters $\theta = (\mu; \sigma)$ are the truth, which is unknown and provide conditional power estimate under various alternatives
 - Based upon initial assumptions for $(\mu; \sigma)$
 - Based upon the observed values at interim (maximum likelihood estimate)
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 - If initial assumptions were optimistic, (1) will delay the stop
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Bayesian Predictive probability³

$$\bullet P(\text{Success}) = \int_{\theta} P(\text{Success}|\theta).P(\theta|Data_{obs} \text{ at } IA)d\theta = \int_{\theta} P(\text{Success}|\theta).P(Data_{obs} \text{ at } IA|\theta).P(\theta)d\theta$$

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60	0.49	0.1
70	0.46	0.05

- Much better for decision making !
- Take into account
 - the current estimates
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First Part summary

- **Go/NoGo criteria** needs to be defined upfront
- Bayesian methods allow proper **quantification** of the benefit/risk (using **clinically relevant threshold** and/or cost function)
- **Prior information** "naturally" included per iterative process of learning
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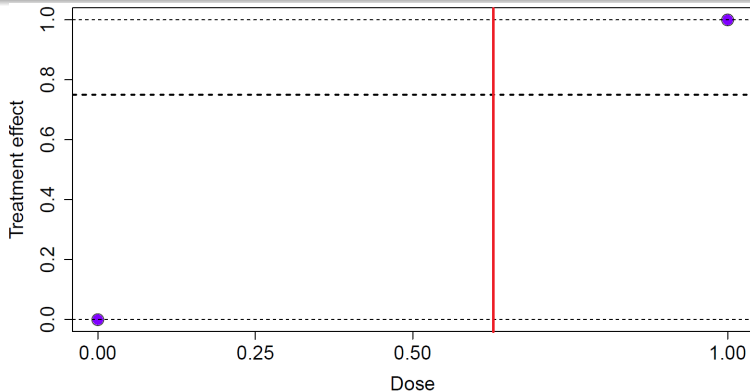
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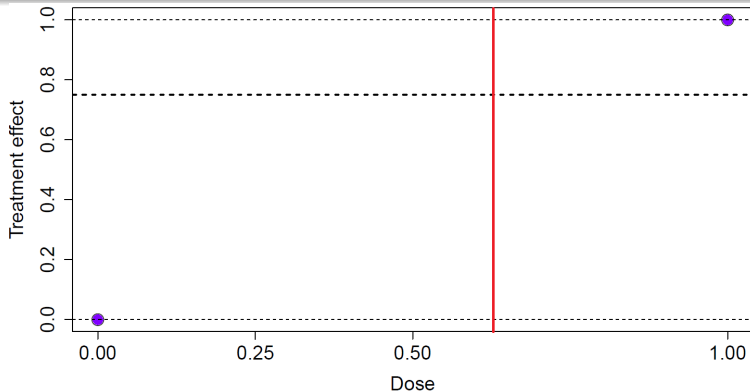
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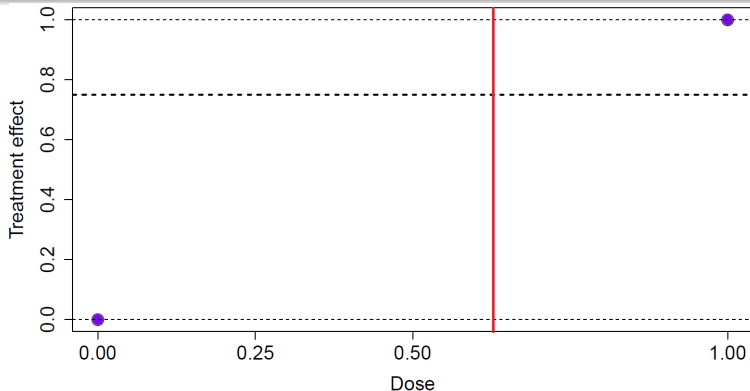
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- 3 Leveraging the information
- 4 Efficiency and cost-effectiveness: adaptive design
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 - Which dose for the next development steps ?
 - And if unacceptable safety above dose 0.6 ?
- ⇒ We can answer with a multi-arms design, getting a rough idea of a "therapeutic window"

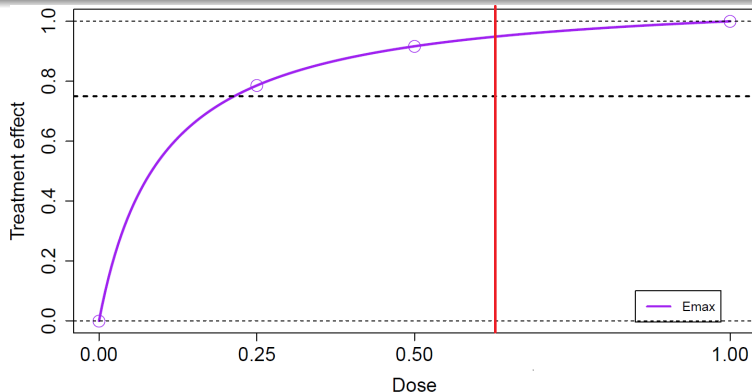


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Dose reponse is of primary importance from a pharmacological point of view

- For learning and next development steps
- Especially in case of suspected U shape

By doing a 2 arms PoC at MTD...

- ✓ We go fast and cheap
- ✓ We do not waste resources on a compound that is not promising
- ✗ We make strong assumption in choosing a dose which yields the targeted effect
- ✗ Do not characterize the dose-response curve
- ✗ We take the risk to conclude on a bad efficacy/risk ratio and so to stop a promising compound

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Alternative strategy is to include **multiple dose levels**

- Mitigates risk of false PoC failure due to incorrect dose
- PoC can be tested via several prespecified dose-response candidate model
 - Mitigates risk of false PoC failure due to incorrect dose-response model
 - Analysis adaptive approach
- Provides information to guide subsequent dose selection
 - Better characterize the "therapeutic window"
 - Reduce the risk of selecting the wrong dose
 - Dose-finding still required but can leverage PoC data
- Usually requires modest increase in sample size vs. 2-arm
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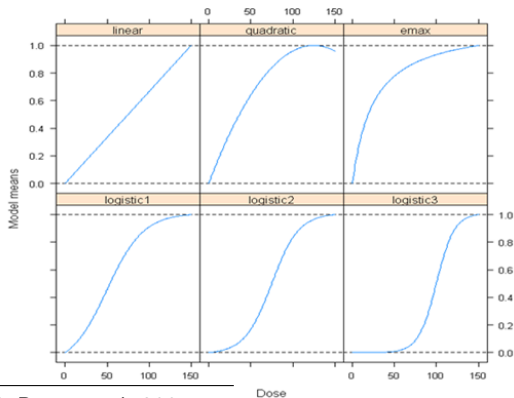
PoC can be demonstrated by **positive dose-response relationship** or precision objective

From **candidate models defined in the protocol**⁴

- 1 Show that a **significant dose-effect** exist using contrast tests while controlling the family-wise error rate (at 5%)
 - The multiplicity issue is solved by a numerical approach taking into account the correlation between models
 - Retain models above a critical value
- 2 If yes, **fit model on data** (AIC \rightarrow weight) and eventually calculate the dose of interest (MED, ED50, ED90) from the selected model(s)
 - By model selection or model averaging (frequentist or bayesian, taking into account the uncertainty of the selection process itself)

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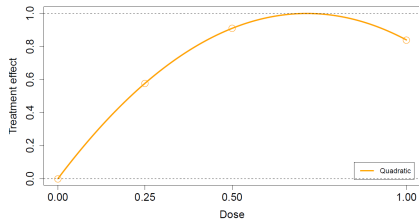
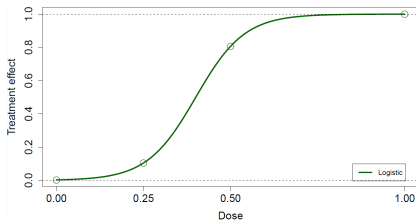
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Case study

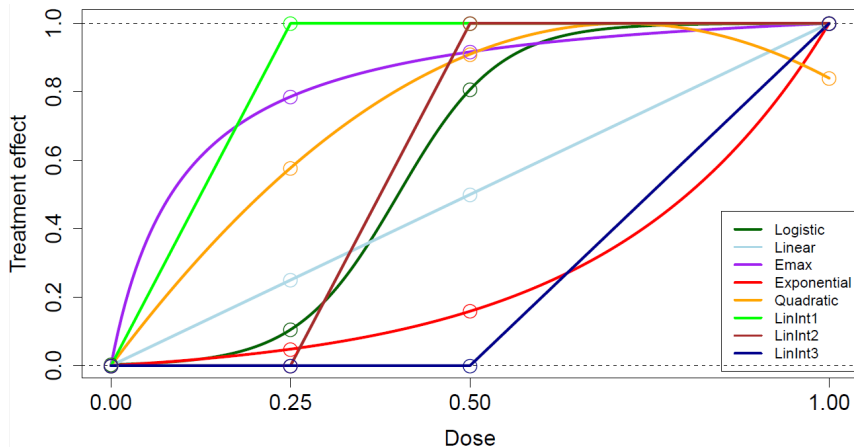
- Placebo + 3 actives dose = $\{0; 0.25; 0.5; 1\}$; $\alpha = 0.05$
one-sided
- Unbalanced randomization 3:1:1:3
- Maximal ES = 1.67 (SD=0.6)
- 2 arms design (N=18) ANOVA vs 4 arms design (N=24)
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Case study : Candidate models



Case study : Results

Table : Power results

Analysis	Sample Size	Design	True Dose response	Power
Anova	18	{9; 0; 0; 9}	Logistic	95.8%
			Quadratic	88.4%
Anova	24	{12; 0; 0; 12}	Logistic	98%
			Quadratic	95%
MCP-mod	24	{9; 3; 3; 9}		92.5% (87.4%-95.6%)

Case study : Conclusions

- Detect a dose-response : evidence of activity represented by a change in clinical response from a change in dose (PoC)
- Estimate the dose-response
 - One can determine if a predefined clinically relevant response could be obtained within the dose-range
 - One can select (interpolate) a targeted dose
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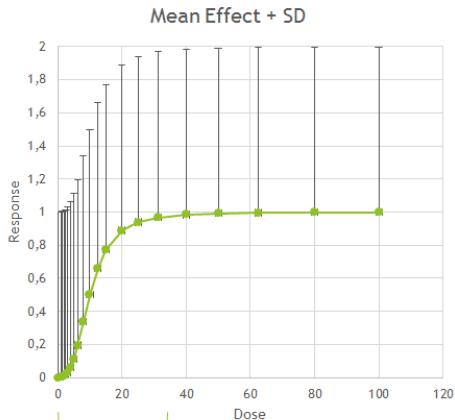
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Case study from

- Compound at end of phase I
 - Maximum dose of 100mg, determined based on safety and PK
- Phase Ib trial goals
 - Proof of concept
 - Dose finding for phase II
- Adaptive dose-ranging versus control

True Dose-Response Relationship



Informative range

- True Emax model
 - $E_0 = 0$
 - $E_{max} = 1$
 - $ED_{50} = 10$ mg
 - Hill coefficient = 3
- Signal /Noise ratio = 1
- Placebo + 21 available doses from 1 to 100 mg
- Model-based adaptive dosing finding strategy

Trial Objectives and Bayesian Analysis

Trial Objectives

- Drug effect
 - Test $E_{max} > 0$
- Dose response
 - Estimate E_{max} model precisely
- Dose selection
 - Find dose with relevant effect : ED50

Priors

- Informative on E_0 : based on historical data
 - Mean = 0, SD = 0.6
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Adaptive Strategy

- Enroll subjects in small successive cohorts & perform dose-response modeling to select doses after each cohort
- First cohort: $N=8$
 - Placebo ($N=2$)
 - 3 dose levels : 1, 10, 100mg ($N=2/\text{dose}$)
- Next cohorts ($N=8$):
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- Decision criteria & stopping rules
 - $Pr(E_{max} > 0) > 95\%$: drug effect
 - Precision of ED50: $CV < 30\%$
 - Stop after a maximum of 6 cohorts ($N=48$)

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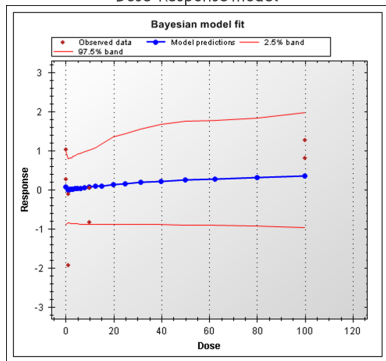
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Adaptive Strategy : After Cohort 1 (N=8)

Dose-Response model

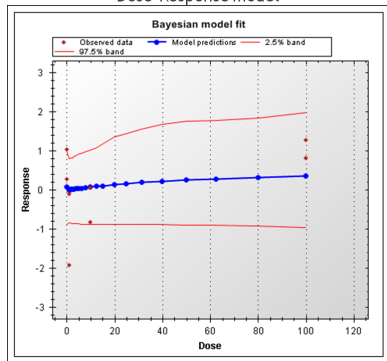


X $\Pr(E_{\max} > 0) = 56\%$

⇒ Continue to cohort 2

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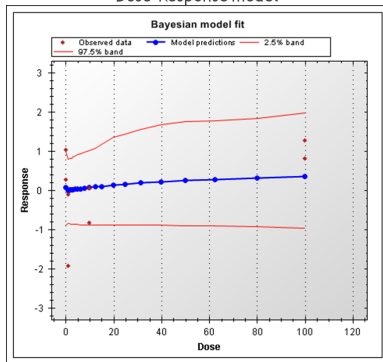


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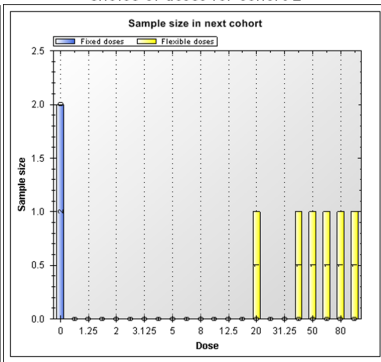
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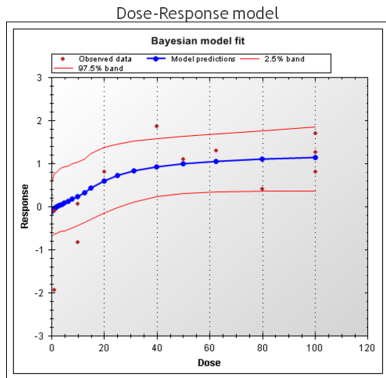
Choice of doses for cohort 2



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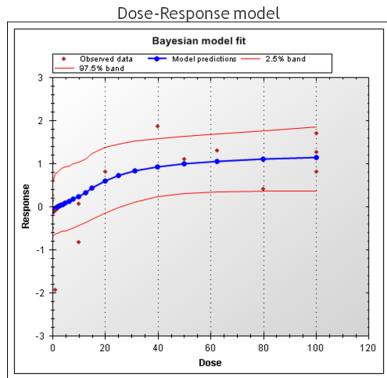


✓ $\Pr(E_{max} > 0) = 99\%$: Proof of concept achieved !

✗ $CV(ED_{50}) = 83\%$

⇒ Continue to cohort 3

Adaptive Strategy : After Cohort 2 (N=16)



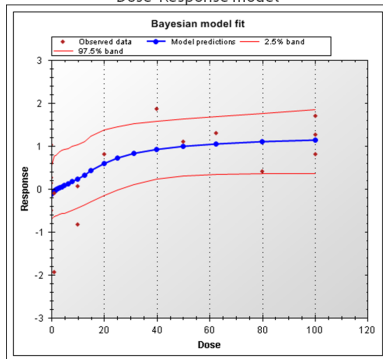
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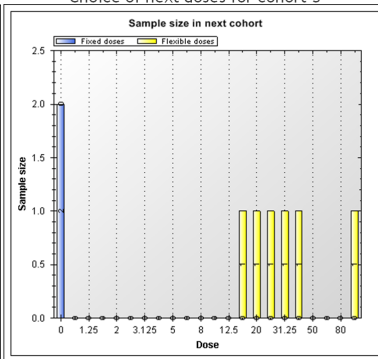
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Dose-Response model



Choice of next doses for cohort 3

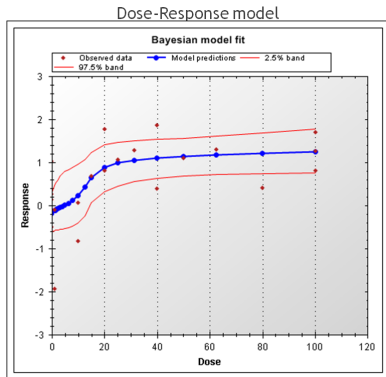


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Adaptive Strategy : After Cohort 3 (N=24)

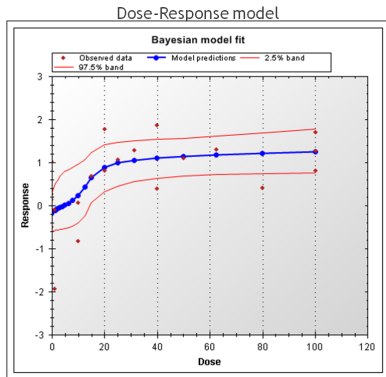


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⇒ Continue to cohort 4

Adaptive Strategy : After Cohort 3 (N=24)



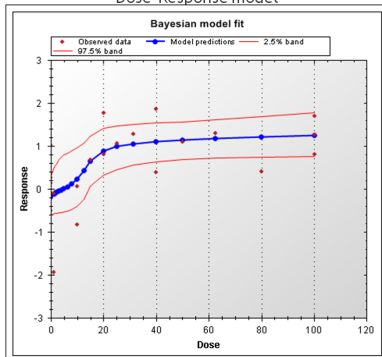
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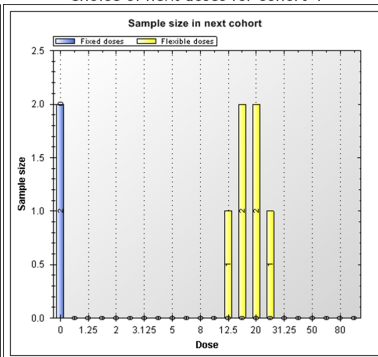
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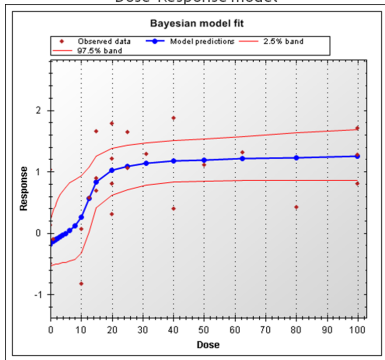
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Adaptive Strategy : After Cohort 4 (N=32)

Dose-Response model



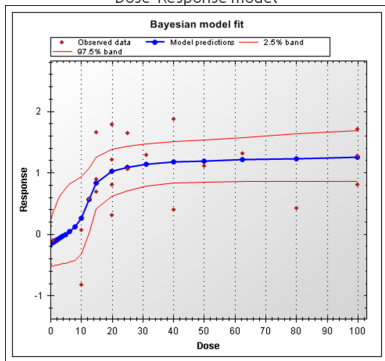
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⇒ Stop trial after 32 subjects

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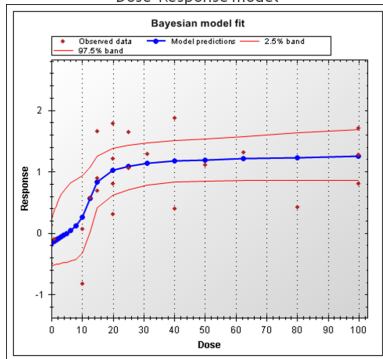
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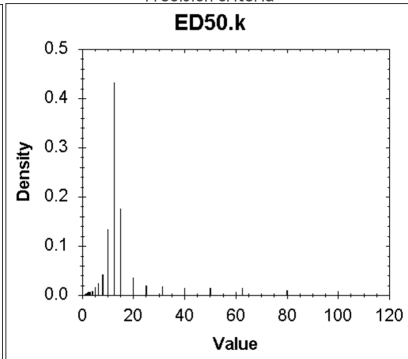
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Precision criteria



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Adaptive Strategy : Results

Emax model estimated with 32 subjects

- $E_0 = -0.2(0.2)$
- $E_{max} = 1.5(0.5)$
- $ED_{50} = 12.5mg(CV = 30\%)$
- $Hill = 4.5(6.6)$

Conclusion

- PoC & dose finding with limited sample size
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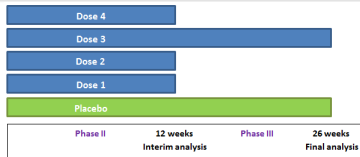
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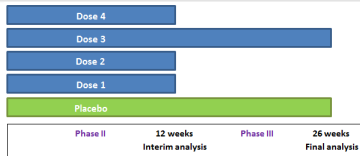
Design that addresses within a **single trial** objectives that are normally achieved through **separate trials** of clinical development



- Advantages
 - Reduce execution timelines
 - Increase final analysis with first stage data (if inferentially)
- Drawbacks
 - Longer protocol preparation; important planning
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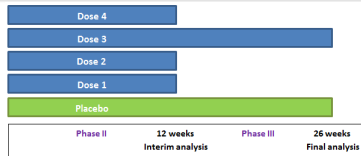
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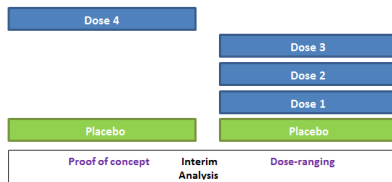
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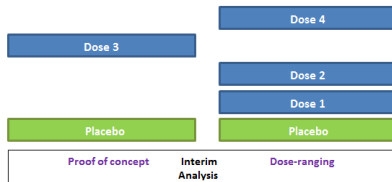
Figure : Stage 1=PoC (unbalanced)/Stage 2=dose-ranging or dose expansion



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 - More flexible : possibility to learn and adapt
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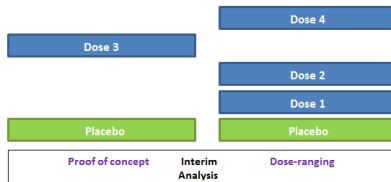
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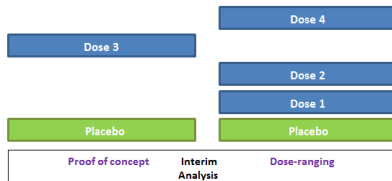
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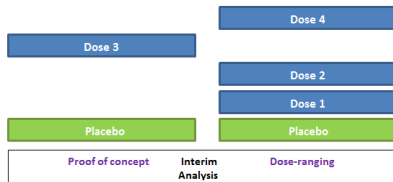
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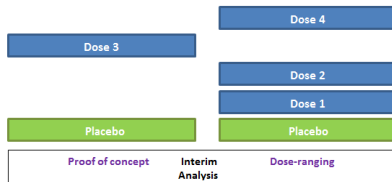
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- 2 Risks considerations
- 3 Leveraging the information
- 4 Efficiency and cost-effectiveness: adaptive design
- 5 About dose-response characterisation
- 6 Summary and discussions**

The Toolbox

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